# Estimation of Trapped Charge Density in SONOS Flash Memory Using a Parallel Capacitor Model

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*Abstract*—This paper proposes a model established using the parallel connection of MOS and floating-gate MOS capacitors to examine the electric properties of polysilicon–oxide– nitride–oxide–silicon (SONOS) Flash memory in both the fresh and programmed states. A linear relationship between threshold voltage shift and effective trapped charge density was revealed via the threshold electric field. The simulation of the channel current was given based on our model, being in agreement with the experimental results for both forward and reverse read modes. The model and theory make an easy and time-saving approach to comprehensively analyze the trapped charge and its effect on other electric properties, e.g., electric field, oxide capacitance, and charge distribution, contributing to the control of the write/erase operation, the optimization of the device structure, and the characteristics of the retention properties in SONOS Flash memory.

*Index Terms*—Polysilicon–oxide–nitride–oxide–silicon (SONOS), threshold electric field, threshold voltage shift, trapped charge density.

## I. INTRODUCTION

HE CHARGE distribution and energy level of the trapped L charge from channel hot-electron injection (CHEI) are essential parameters affecting the cell endurance and scalability of polysilicon (poly-Si)-oxide-nitride-oxide-silicon (SONOS) Flash memory [1]–[3]. The spatial distribution of the trapped charge has been extensively examined using a variety of approaches, e.g., quasi-2-D analytical model [4], gate-induceddrain-leakage simulation, charge pumping [5], analysis of current transient, threshold voltage, and subthreshold slope (SS) [6]–[8]. Both the bulk and the interface trap depth in SONOS devices have been examined using capacitance–voltage (C-V)measurements and deep-level transient spectroscopy (DLTS) [9]. Electron retention in stacked dielectrics has been also modeled using a thermal emission mechanism [10]. However, the relations between the trapped charge density and the other electric properties, e.g., electric field, oxide capacitance, and charge distribution, have not been clearly investigated in the previous studies. These relations are essential for comprehen-

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sively understanding the influence of the trapped charge on the electrical performance, i.e., the control of the write/erase (W/E) operation, the optimization of the device structure, and the characterization of the retention properties in SONOS devices [11], [12].

In this paper, an equivalent model established by the parallel connection of MOS and floating-gate MOS capacitors was proposed for characterization of the trapped charge in SONOS memory devices. Threshold voltage shift  $\Delta V_{\rm th}$  was obtained as a linear function of effective trapped charge density  $\overline{\sigma}_t$  using threshold electric field  $E_{\rm th}$ , which was proposed as a signature for the formation of the inversion channel in order to link the threshold voltage in both fresh and programmed states. A comprehensive analysis of various electrical properties was carried out as a function of the gate voltage, providing the relations between the trapped charge density and the electric field, oxide capacitance, charge distribution, etc. A simulation of the channel current under both forward and reverse read modes was in agreement with experimental results. Compared to previous studies, our model has its own advantages. First,  $E_{\rm th}$  was proposed newly as a key parameter in our model to connect  $V_{\rm th}$  before and after programming, owing to its constant value in both fresh and programmed states. Second, our model provides comprehensive information of various electrical properties, e.g., charge distribution at the gate, trapping layer and substrate, electric field through the block and tunnel oxides, oxide capacitance in the fresh and programmed states, and drain-induced barrier lowering (DIBL) and its effect on the other properties, in which some pieces of information are rarely obtained in conventional approaches. Third, our model is very simple and time saving. According to the experimental  $\Delta V_{\rm th}$ and the derived equations, various properties can be obtained via simple calculations in minutes. Finally, our model has the potential for wide applications, e.g., the control of the W/E operation, the optimization of the device structure, and the characterization of the retention properties. In addition, it can be modified and applied to the SONOS cells using various trapping materials or the modeling of the split-gate SONOS cells using separated charge-storage nodes. These indicate the parallel capacitor model to be an effective and convincing approach for a comprehensive analysis of the trapped charge in SONOS memory devices.

#### II. DEVICE FABRICATION AND ELECTRICAL ANALYSIS

The SONOS memory device was fabricated using a standard complementary metal–oxide–semiconductor process with a poly-Si/SiO<sub>2</sub>/HfO<sub>2</sub>/SiO<sub>2</sub>/Si gate stack. After the thermal



Fig. 1. (a) Illustration of the SONOS model formed by two capacitors, i.e.,  $C_1$  and  $C_2$ , connected in parallel. (b) Experimental result of I-V characteristics under the forward read mode for various  $V_D$  levels (0.1, 0.6, 1.1, and 1.6 V) before (hollow symbol) and after (solid symbol) programming.

growth of a 3-nm-thick tunnel oxide d on p-type Si substrate, a 6-nm-thick HfO<sub>2</sub> film with an effective oxide thickness (EOT) of ~1 nm was deposited by sputtering. A 9-nm-thick block oxide was deposited, followed by the deposition of 180-nmthick poly-Si. The device has a physical gate length  $L_{\rm eff}$  of 200 nm, a channel width W of 2  $\mu$ m, and an EOT of the SiO<sub>2</sub>/HfO<sub>2</sub>/SiO<sub>2</sub> stack D of 13 nm, as shown in Fig. 1(a). The channel current–gate voltage (I–V) characteristics under both forward and reverse read modes were carried out before and after CHEI programming at an applied gate voltage V<sub>G</sub> of 5 V and a drain voltage V<sub>D</sub> of 10 V for 1 ms with the source and substrate grounded, as shown in Fig. 1(b).

#### III. MODELING AND THEORY

The following assumptions are made to establish the parallel capacitor model.

1) The charge at the gate, trapping layer, and substrate are uniformly distributed over the surface, generating their corresponding uniform electric fields as

$$E = \frac{\overline{\sigma}}{\varepsilon_{\rm ox}} \tag{1}$$

where  $\overline{\sigma}$  is the average or effective charge density,  $\varepsilon_{\text{ox}}$  is the permittivity of SiO<sub>2</sub>, and the direction of *E* is perpendicular to the charge surface.

- 2) The charge density of the inversion channel  $\sigma_i$  is neglected when the gate voltage is less than the threshold voltage ( $V_G < V_{\rm th}$ ) [13] because the strong inversion condition is not reached. The only uncompensated charge in the Si substrate is due to the doped ions in the depletion layer.
- 3) When the gate voltage is greater than the threshold voltage  $(V_G > V_{\rm th})$ , the surface potential  $\varphi_s$  and, consequently, the charge density in the depletion layer  $\sigma_d$  are constant, which can be expressed as  $\varphi_s = 2\phi_F$  and  $\sigma_d = 2\sqrt{\phi_F \varepsilon_{\rm Si} q N_A}$  [13], respectively, where  $\phi_F$  is the Fermi level,  $\varepsilon_{\rm Si}$  is the permittivity of Si, q is the unit of charge, and  $N_A$  is the substrate doping concentration. The gate voltage beyond the threshold voltage  $(V_G V_{\rm th})$  is used to form an inversion layer as  $\sigma_i = (V_G V_{\rm th})C_{\rm ox}$ , where  $C_{\rm ox}$  is the oxide capacitance.

When the gate voltage is equal to the threshold voltage  $(V_G = V_{\rm th})$ , the electric field at the substrate surface reaches  $E_{\rm th}$ , which is defined as a vertical electric field needed to form the inversion channel. The value of  $E_{\rm th}$  is only determined by the substrate doping concentration, and thereby, it is the same before and after CHEI programming. This is a unique advantage compared to  $V_{\rm th}$ , and it is used to link  $V_{\rm th}$  in both fresh and programmed states. In this model, the fresh SONOS cell is analyzed in an equivalent manner to the MOSFET device, where  $E_{\rm th}$  is defined by the threshold voltage in the fresh state  $(V_{\rm th(fresh)})$  as

$$E_{\rm th} = \frac{V_{\rm th(fresh)}}{D} \tag{2}$$

and the average charge density at the bottom of poly-Si is  $\overline{\sigma}_1$ , generating its electric field  $E_1$  as  $\overline{\sigma}_1/\varepsilon_{\text{ox}}$ . The programmed SONOS cell is considered a MOS capacitor  $C_1$  (0 < x < L - l) and a floating-gate MOS capacitor  $C_2$  (L - l < x < L) in a parallel connection [see Fig. 1(a)]. Since CHEI occurs near the drain end [7],  $C_1$  is unaffected and its average gate charge density and electric field are equal to  $\overline{\sigma}_1$  and  $E_1$ , respectively. In  $C_2$ , the injected charges are assumed to be trapped at the bottom of the trapping layer as  $\overline{\sigma}_t$ , establishing its electric field  $E_t$  of  $\overline{\sigma}_t/\varepsilon_{\text{ox}}$ . The average gate charge density becomes  $\overline{\sigma}_2$  with an established electric field  $E_2$  of  $\overline{\sigma}_2/\varepsilon_{\text{ox}}$ .

First, the electric fields through the block oxide (0 < y < D - d) and the tunnel oxide (D - d < y < D) in  $C_2$  are estimated using the principle of superposition as  $E_{(\text{block})} = E_2 + E_t = (\overline{\sigma}_2 + \overline{\sigma}_t)/\varepsilon_{\text{ox}}$  and  $E_{(\text{tunnel})} = E_2 - E_t = (\overline{\sigma}_2 - \overline{\sigma}_t)/\varepsilon_{\text{ox}}$ , respectively. Second, due to the parallel connection,  $V_G$  in  $C_2$  as  $\int_0^{D-d} E_{(\text{block})} dy + \int_{D-d}^D E_{(\text{tunnel})} dy$  is equal to that in  $C_1$  as  $\int_0^D E_1 dy$ . Therefore, the relationships of  $\overline{\sigma}_1, \overline{\sigma}_2$ , and  $\overline{\sigma}_t$  are obtained as

$$\overline{\sigma}_1 = \frac{\varepsilon_{\rm ox}}{D} V_G \tag{3}$$

$$\overline{\sigma}_2 = \overline{\sigma}_1 - \frac{D - 2d}{D}\overline{\sigma}_t.$$
(4)

Assuming that  $\overline{\sigma}_t$  is infinitely small,  $\overline{\sigma}_2$  would be the same as  $\overline{\sigma}_1$ , which is consistent with the experimental results. Third, according to (4), the electric fields through the block and tunnel oxides are rewritten as follows:

$$E_{\text{(block)}} = \frac{V_G}{D} + \frac{2d}{D} \cdot \frac{\overline{\sigma}_t}{\varepsilon_{\text{ox}}}$$
(5)

$$E_{(\text{tunnel})} = \frac{V_G}{D} - \frac{2(D-d)}{D} \cdot \frac{\overline{\sigma}_t}{\varepsilon_{\text{ox}}}.$$
 (6)

Since the formation of the conducting channel at the interface is induced only by  $E_{(\text{tunnel})}$ , it is reasonable to assume that  $E_{(\text{tunnel})} = E_{\text{th}}$  when  $V_G$  reaches the threshold voltage in the programmed state  $V_{\text{th}(\text{prog})}$ . Therefore, the threshold voltage shift, i.e.,  $\Delta V_{\text{th}} = V_{\text{th}(\text{prog})} - V_{\text{th}(\text{fresh})}$ , can be obtained as follows:

$$\Delta V_{\rm th} = 2(D-d)\frac{\overline{\sigma}_t}{\varepsilon_{\rm ox}}.$$
(7)

Equation (7) (which can be also represented with the capacitance of the block oxide  $C_{\text{block}}$  as  $\Delta V_{\text{th}} = 2\overline{\sigma}_t/C_{\text{block}}$ ) shows that  $\Delta V_{\text{th}}$  is a linear function of  $\overline{\sigma}_t$ , as well as the distance between the trapped charge and the gate electrode. Compared with the conventional expression as  $\Delta V_{\text{th}} = \overline{\sigma}_t/C_{\text{block}}$  [11] for the bulk trapping layer in which the charge on the top surface is considered to interact with the gate, there is a coefficient "2" in our formula due to the assumption of the zero-thickness charge sheet that provides the double interaction with both gate and substrate. Assuming a more complicated model, where the thickness of the trapping layer is included and the charge density on the top and bottom surfaces is individually considered, the same expression as  $\Delta V_{\text{th}} = \overline{\sigma}_t/C_{\text{block}}$  can be still derived in our approach.

According to the experimental value of  $\Delta V_{\text{th}}$  [see Fig. 1(b)], the electric properties, e.g., electric field, oxide capacitance, charge distribution at the gate, inversion channel, and depletion region, are obtained by combining (7) with their corresponding equations. For example, the expressions of  $E_{(block)}$  and  $E_{\text{(tunnel)}}$  [see (5) and (6)] are rewritten as  $[V_G + d\Delta V_{\text{th}}/(D - d\Delta V_{\text{th}})]$ d)]/D and  $(V_G - \Delta V_{\rm th})/D$ , respectively, which are shown in Fig. 2.  $E_{\rm th}$  is a constant of  $1.06 \times 10^8$  V/m, determined by (2).  $E_1, E_{(block)}$ , and  $E_{(tunnel)}$  are expressed as linear functions of  $V_G$  (0–12 V) for various  $V_D$  (0.1, 0.6, 1.1, and 1.6 V) levels. In the fresh state, the location of the intersection between  $E_{\rm th}$ and  $E_1$  (point A) indicates its corresponding  $V_{\rm th(fresh)}$ . As a comparison,  $E_{(block)}$  becomes higher and  $E_{(tunnel)}$  becomes lower than  $E_1$  in the programmed state for the same  $V_G$ condition due to the influence of the negative trapped charges. Therefore,  $V_{\rm th(prog)}$  requires a higher value for compensation to make  $E_{(\text{tunnel})}$  equal to  $E_{\text{th}}$ , as indicated by the locations of the intersection between  $E_{\rm th}$  and  $E_{\rm (tunnel)}$  (points B–E). In addition, the distribution of the electric field along the yaxis is also shown in the inset, suggesting that  $E_1$  is equal to  $E_{\rm th}$  for  $V_G = V_{\rm th(fresh)}$ , and  $E_{\rm (tunnel)}$  is equal to  $E_{\rm th}$  for  $V_G = V_{\text{th}(\text{prog})}.$ 

The oxide capacitance for  $C_2$  in the programmed state is expressed as  $C_{\text{ox}(\text{prog})2} = \overline{\sigma}_2/V_G = \varepsilon_{\text{ox}}/[D + (D - 2d)\overline{\sigma}_t/\overline{\sigma}_2]$ , which is smaller than that for the fresh state or  $C_1$  in the pro-



Fig. 2. Estimation of the electric field  $E_{\rm (block)}$  (hollow symbol) and  $E_{\rm (tunnel)}$  (solid symbol) as a function of  $V_G$ , as compared to  $E_1$  (solid line) and  $E_{\rm th}$  (dashed line). The location of the intersection between  $E_{\rm th}$  and  $E_1$  (point A) indicates its corresponding  $V_{\rm th(fresh)}$ . The location of the intersection between  $E_{\rm th}$  and  $E_{\rm (tunnel)}$  (points B–E) indicates its corresponding  $V_{\rm th(fresh)}$ . The location of the intersection between  $E_{\rm th}$  and  $E_{\rm (tunnel)}$  (points B–E) indicates its corresponding  $V_{\rm th(prog)}$  for various  $V_D$  levels, being consistent with the experimental results. The electric field distribution along the y-axis when  $V_G = V_{\rm th(fresh)}$  and  $V_G = V_{\rm th(prog)}$  is shown in the inset.



Fig. 3. Estimation of the oxide capacitance  $C_{\text{ox}(\text{prog})}$  or  $C_{\text{ox}(\text{prog})1}$  (hollow symbol) and  $C_{\text{ox}(\text{prog})2}$  (solid symbol) as a function of  $V_G$  with their distribution along the x-axis under the same  $V_G$ , as shown in the inset.

grammed state obtained as  $C_{\text{ox}(\text{fresh})} = C_{\text{ox}(\text{prog})1} = \overline{\sigma}_1/V_G = \varepsilon_{\text{ox}}/D$ , as shown in Fig. 3.  $C_{\text{ox}(\text{prog})2}$  increases close to  $C_{\text{ox}(\text{prog})1}$  with increasing  $V_G$ , owing to the increase in  $V_G$ -dependent  $\overline{\sigma}_2$ . The distribution of the oxide capacitance along the x-axis is also shown in the inset, suggesting a reduction of the oxide capacitance in the region where the trapped charge occupied (from  $L_{\text{eff}} - l$  to  $L_{\text{eff}}$ ).

The charge distributions at the trapping layer, gate, and inversion channel are shown in Fig. 4.  $\overline{\sigma}_t$  is obtained by (7), showing independence of  $V_G$ . Due to its effect,  $\overline{\sigma}_2$  that is obtained as a function of  $V_G$  [see (4) and (7)] becomes smaller than  $\overline{\sigma}_1$  [see (3)] for the same  $V_G$  condition, as shown in Fig. 4(a). Based on the oxide capacitance (see Fig. 3), the charge densities at the inversion channel in the fresh state  $\overline{\sigma}_{i(\text{fresh})}$  (or for  $C_1$  in the programmed state  $\overline{\sigma}_{i(\text{prog})1}$ ) and for  $C_2$  in the programmed state  $\overline{\sigma}_{i(\text{prog})2}$  are expressed as  $(V_G - V_{\text{th}(\text{fresh})})C_{\text{ox}(\text{fresh})}$  and  $(V_G - V_{\text{th}(\text{prog})2})C_{\text{ox}(\text{prog})2}$ , respectively, as shown in Fig. 4(b).  $\overline{\sigma}_{i(\text{prog})2}$  becomes smaller than  $\overline{\sigma}_{i(\text{prog})1}$  for the same  $V_G$  condition due to the reduction of  $C_{\text{ox}(\text{prog})2}$  compared with  $C_{\text{ox}(\text{prog})1}$ , and therefore, it requires



Fig. 4. (a) Estimation of the charge density  $\overline{\sigma}_1$  (solid line),  $\overline{\sigma}_2$  (solid symbol), and  $\overline{\sigma}_t$  (hollow symbol) as a function of  $V_G$ . The charge distribution along the *y*-axis under the same  $V_G$  is shown in the inset, where  $\overline{\sigma}_2$  and  $\overline{\sigma}_i$  after programming are reduced due to the injected  $\overline{\sigma}_t$ . (b) Estimation of the charge density  $\overline{\sigma}_i(\text{fresh})$  or  $\overline{\sigma}_i(\text{prog})_1$  (hollow symbol) and  $\overline{\sigma}_i(\text{prog})_2$  (solid symbol) as a function of  $V_G$  with their distribution along the *x*-axis under the same  $V_G$ , as shown in the inset. The charge density in the depletion region  $\overline{\sigma}_d$  (solid line) is also shown.

a higher  $V_G$  for compensation to form the inversion channel. The charge distributions along the y- and x-axes are shown in the insets in Fig. 4(a) and (b), respectively, suggesting a reduction of the charge density at the gate and the inversion layer where the trapped charge occupied (from  $L_{\rm eff} - l$  to  $L_{\rm eff}$ ).

Moreover, DIBL is clearly observed via the reduction of  $\overline{\sigma}_t$  from  $8.80 \times 10^{-3}$  to  $3.11 \times 10^{-3}$  C/m<sup>2</sup> by increasing  $V_D$  from 0.1 to 1.6 V [see Fig. 4(a)]. In the meantime, the effect of the DIBL on the other electric properties, e.g., the trapped charge-induced differences between the electric fields  $E_{\text{(block)}}$  and  $E_{\text{(tunnel)}}$ , oxide capacitance values  $C_{\text{ox(prog)1}}$  and  $C_{\text{ox(prog)2}}$ , charge distributions  $\overline{\sigma}_1$  and  $\overline{\sigma}_2$ , and  $\overline{\sigma}_{i(\text{prog)1}}$  and  $\overline{\sigma}_{i(\text{prog)2}}$ , is gradually and clearly reduced (see Figs. 2–4).

#### **IV. CHANNEL CURRENT SIMULATION**

Considering the effect of  $V_D$  that causes a nonuniform distribution of the inversion layer charge density along the channel, the varying threshold voltage in the fresh SONOS device  $(v_{\rm th(fresh)})$  can be expressed in terms of the surface potential variation as  $V_{\rm FB} + \varphi_s + (2\varepsilon_{\rm Si}qN_A\varphi_s)^{1/2}/C_{\rm ox(fresh)}$ , where  $V_{\rm FB}$  is the flatband voltage, and  $N_A$  is the acceptor concentration of the Si substrate. The drain current is obtained by the simulation of a MOSFET device via Simulation Program with Integrated Circuit Emphasis (SPICE) Level 2 model [13]. For the programmed SONOS device, the threshold voltage in  $C_1$  ( $v_{\rm th(prog)1}$ ) can be still expressed as  $v_{\rm th(fresh)}$ . However, it is affected by the trapped negative charges in  $C_2$  and is expressed as follows:

l

$$\begin{aligned}
\psi_{\rm th(prog)2} &= v_{\rm th(fresh)} + \Delta V_{\rm th} \\
&= V_{\rm FB} + \varphi_s + \frac{\sqrt{2\varepsilon_{\rm Si}qN_A}}{C_{\rm ox(fresh)}} \sqrt{\varphi_s} + \Delta V_{\rm th}. \quad (8)
\end{aligned}$$

Therefore, the average charge density of the inversion layer is obtained by combining capacitors  $C_1$  and  $C_2$  with their corresponding threshold voltages when  $\varphi_s$  was varied from  $2\phi_F$  at the source end to  $2\phi_F + V_D$  at the drain end [see Fig. 1(a)] as follows:

$$\overline{\sigma}_{i} = \frac{1}{V_{D}} \int_{2\phi_{F}}^{2\phi_{F}+V_{D}} [V_{G} - v_{\mathrm{th}}(\varphi_{s})] C_{\mathrm{ox}} d\varphi_{s}$$

$$= \frac{1}{V_{D}} \begin{cases} 2\phi_{F} + (1-l/L_{\mathrm{eff}})V_{D} \\ \int_{2\phi_{F}} [V_{G} - v_{\mathrm{th(fresh)}}] C_{\mathrm{ox(fresh)}} d\varphi_{s} \\ \frac{2\phi_{F} + V_{D}}{2\phi_{F} + (1-l/L_{\mathrm{eff}})V_{D}} [V_{G} - v_{\mathrm{th(prog)}2}] C_{\mathrm{ox(prog)}2} d\varphi_{s} \end{cases}.$$
(9)

The expression of  $\overline{\sigma}_i$  can be obtained by solving the above integral with (8). The drain current after programming, therefore, is obtained as follows [13]:

$$I_{D(\text{prog})} = \frac{\mu_0 W}{L_{\text{eff}}} \overline{\sigma}_i V_D \tag{10}$$

where  $\mu_0$  is the electron mobility. According to (7)–(10), the drain current after programming is affected by the density  $\overline{\sigma}_t$  and the occupied length l of the injected charge in the trapping layer, indicating the height and the width of the potential barrier in the inversion channel, respectively. The simulation results of  $I_D-V_G$  for various  $V_D$  levels in the programmed state are compared with the experimental data, as shown in Fig. 5(a).

In addition, all previous analyses are based on the forward read mode, in which  $V_D$  is applied as a positive voltage and substrate voltage  $V_S$  is grounded. The parallel capacitor model for the reverse read mode is still valid. Assuming that a positive voltage applied to  $V_S$  and  $V_D$  is grounded, (9) can be revised as follows:

$$\overline{\sigma}_{i} = \frac{1}{V_{S}} \int_{2\varphi_{F}+V_{S}}^{2\varphi_{F}} \left[V_{G} - v_{\mathrm{th}}(\varphi_{s})\right] C_{\mathrm{ox}} d\varphi_{s}$$

$$= \frac{1}{V_{S}} \begin{cases} \sum_{2\varphi_{F}+(l/L_{\mathrm{eff}})V_{S}}^{2\varphi_{F}+(l/L_{\mathrm{eff}})V_{S}} \left[V_{G} - v_{\mathrm{th}(\mathrm{fresh})}\right] C_{\mathrm{ox}(\mathrm{fresh})} d\varphi_{s}$$

$$+ \int_{2\varphi_{F}+(l/L_{\mathrm{eff}})V_{S}}^{2\varphi_{F}} \left[V_{G} - v_{\mathrm{th}(\mathrm{prog})2}\right] C_{\mathrm{ox}(\mathrm{prog})2} d\varphi_{s} \end{cases}.$$
(11)

Fig. 5. Comparison of the experimental (solid symbol) and simulated (dashed line) channel current in the programmed state under (a) the forward read mode for various  $V_D$  levels and (b) the reverse read mode for various  $V_S$  levels.

The channel current in the reverse read mode can be expressed as

$$I_{S(\text{prog})} = \frac{\mu_0 W}{L_{\text{eff}}} \overline{\sigma}_i V_S \tag{12}$$

and the simulation results of  $I_S-V_G$  for various  $V_S$  levels in the programmed state are compared with the experimental data, as shown in Fig. 5(b). Compared to the variation of  $V_{\text{th}(\text{prog})}$  as a function of  $V_D$  in the forward read mode, its variation as a function of  $V_S$  in the reverse read mode is not obvious since the charge potential barrier is located at the drain end where the depletion region of the source cannot reach and reduce it when  $V_S$  is not high enough [5].

In addition, our model follows the conventional theory of MOSFET devices, and therefore, a variety of techniques can be included to improve the simulation accuracy. For example, the estimated current density can be improved close to the experimental value by considering channel-length modulation, mobility reduction with gate/drain voltage, subthreshold current, fitting parameter, etc. [4], [13], which give rise to the improvement of the accuracy in future applications.

# V. APPLICATION AND DISCUSSION

Our model gives a comprehensive analysis of SONOS devices, particularly on the relations between the trapped charge density and the electric field, oxide capacitance, charge distribution, etc. For example, the effective trapped charge density is estimated based on the threshold voltage shift [see (7)], and this provides the essential information for the control of the W/E operation. Moreover, compared to the fresh state, the oxide capacitance is reduced in the region where the trapped charge occupied (from  $L_{\rm eff} - l$  to  $L_{\rm eff}$ ), resulting in an insufficient charge density at the substrate surface to form the conducting channel and requiring additional  $\Delta V_{\rm th}$  for compensation. These relations have been clearly provided in our model [see (3)–(7)], and their applications are discussed as follows.

First, since these relations are dependent on the geometry of the oxide stack and the magnitude of  $\Delta V_{\rm th}$ , the information of the electric field, oxide capacitance, and charge distribution can be used for optimizing the device structure and the W/E condition. For example,  $E_{\rm (tunnel)}$  that directly relates to  $E_{\rm th}$  is determined by the geometry of the oxide stack [see (6)], and therefore, the required trapped charge density to achieve  $E_{\rm th}$ can be estimated for a specific device structure.

Second, the retention characteristics can be performed based on our model. For example, the influence from the reduction of the trapped charge density  $(\overline{\sigma}_t)$  can be observed in terms of the variation of the electric field, oxide capacitance, and charge distribution [see (3)–(7)]. In addition, the influence from the shrinkage of the occupied region l can be estimated by the variation of the channel current [see (9)–(12)].

Third, all analyses in our model so far are based on the assumption that the trapped charge is located at the bottom of the trapping layer. The vertical location of  $\overline{\sigma}_t$  is negligible because the trapping layer is quite thin (~1 nm of EOT). Assuming an opposite condition that  $\overline{\sigma}_t$  is located at the top interface, all the equations still work by replacing d with d + 1 in nanometer units, and their corresponding simulation results, which are not shown here, are quite similar to the results shown in Fig. 5(a) and (b). Therefore, the parallel capacitor model could be modified and applied to other SONOS devices using different trapping materials, e.g., Si<sub>3</sub>N<sub>4</sub>, where the trapped charge has been reported to be located at the top SiO<sub>2</sub>/Si<sub>3</sub>N<sub>4</sub> interface [5].

Finally, the parallel capacitor model can be also used to model the split-gate SONOS device [14]. Because the trapped charges are separately located at the drain and source ends, the cell is equivalently modeled as a parallel connection of three capacitors, i.e., two floating-gate MOS capacitors at the channel ends and one MOS capacitor in the middle. Their electric properties can be individually obtained in the corresponding capacitor, and their combinations are used to model the electrical performance of the entire device, such as the channel current in both read modes.

### VI. CONCLUSION

In this paper, the parallel capacitor model has been proposed as a quite simple and time-saving approach to comprehensively analyze the electric properties of the SONOS memory device, including the charge density at the gate, trapping layer and substrate, electric field through the block and tunnel oxides, oxide capacitance in both fresh and programmed states, as well as channel current in both forward and reverse read modes. Our



model can be applied for the control of the W/E operation, the optimization of the device structure, and the characterization of the retention properties in SONOS Flash memory.

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