

# Metal–Insulator Transition Driven by Traps in 2D WSe<sub>2</sub> Field-Effect Transistor

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Localized trap density  $(D_t)$  at the 2D channel-gate dielectric interface and its relative strength to carrier-carrier interactions depending on the thickness of the 2D channel can determine the nature of a metal-insulator transition (MIT) in 2D materials. Here, the MIT occurring in WSe<sub>2</sub> devices is systematically analyzed by varying the WSe<sub>2</sub> thickness from ≈20 nm to monolayer to explore the effects of Dt on MIT. The corresponding critical carrier density increases from  $\approx 8.30 \times 10^{11}$  to  $9.45 \times 10^{12}$  cm<sup>-2</sup> and D<sub>t</sub> from  $\approx$ 6.02  $\times$  10<sup>11</sup> to 1.13  $\times$  10<sup>13</sup> cm<sup>-2</sup> eV<sup>-1</sup> as WSe<sub>2</sub> thickness decreases from ≈20 nm to monolayer. These large increments in Dt with decreasing thickness of WSe<sub>2</sub> induce a strong potential fluctuation in the band of WSe<sub>2</sub>, causing charge density inhomogeneity in the system, which attributed to tuning the MIT. The critical percolation exponent is strongly dependent on WSe<sub>2</sub> thickness with an excellent agreement between the transport data and percolation theory achieved from thinner WSe<sub>2</sub> devices, while the transport data measured from multilayer WSe2 devices does not obey the percolation theory. These results suggest that the nature of MIT strongly depends on the WSe<sub>2</sub> channel thickness and corresponding unscreened charge impurity and strength of  $D_{t}$  at the interface.

## **1. Introduction**

Technically, atomically thin 2D materials are all surfaces and interfaces.<sup>[1–5]</sup> Therefore, 2D materials-based devices exhibit a trap density ( $D_t$ ) of  $\approx 10^{13} - 10^{12}$  cm<sup>-2</sup> eV<sup>-1</sup> that is several orders higher than that of high-quality channel-gate dielectric interfaces at <10<sup>10</sup> cm<sup>-2</sup> eV<sup>-1</sup>.<sup>[6,7]</sup> Thus, the intrinsic characteristics of 2D material-based devices are readily tailored by their interfacial quality.<sup>[8,9]</sup> More specifically, carrier transport within a channel is significantly influenced by the localized state commonly known as the trap states at the 2D channel–gate dielectric interface by inducing transport through interface

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trap charges.<sup>[7,10]</sup> These electrically active interface traps can adversely affect device performance by reducing charge carrier mobility, increasing subthreshold swing, and enhancing off-state current (reducing on/off ratio).<sup>[7]</sup> In addition, these charge impurities near the surface of 2D materials and different kinds of disorders can strongly suppress electronic interactions and control the electrical characteristics of the system.<sup>[11-13]</sup> Since the pioneering observation of metal-insulator transition (MIT) phenomena in 2D systems, carrier-carrier interaction has been widely considered as the driving force of MIT from the viewpoint of quantum phase transition.<sup>[14-16]</sup> However, the previous theories suggested that the relative strength of D<sub>t</sub> and carrier-carrier interaction in the system determine the physical origin of MIT.<sup>[17-20]</sup> In 2D layer materials, the strength of carrier-carrier interaction and disorders induced by interface traps, and defects can be modulated by controlling

the thickness of the 2D channel, substrate engineering, and surface passivation.<sup>[2,21]</sup> In general, carrier–carrier interactions decrease with reducing thickness while localized  $D_t$  increases significantly. Therefore, different kinds of transition mechanisms in 2D layered materials are expected depending on the thickness of the flake and the corresponding interface quality. Previously, it has been reported that the  $D_t$  drastically increases when employing thin flakes since thinner 2D flakes are more susceptible to interface disorders than their thicker counterparts.<sup>[6,7,22]</sup> Thus, it is difficult to correctly identify the origin of MIT in a 2D material system when both carrier-carrier interactions and a large amount of localized trap states ( $\approx 10^{13}$  cm<sup>-2</sup> eV<sup>-1</sup>) induced from the channel and channel–gate dielectric interface effects come into play.

In the past, some efforts have been made to explain the MIT in 2D  $MoS_2$ ,<sup>[23–26]</sup>  $ReS_2$ ,<sup>[27]</sup> CuInSe,<sup>[28]</sup> and  $WSe_2$ .<sup>[29]</sup> However, most of these studies were limited to a certain channel thickness. Although a few studies have reported MIT in 2D materials,<sup>[23,26–30]</sup> how localized  $D_t$  interplays near a transition point with varying thickness of 2D flakes remains unclear. There is a need to systematically analyze the underlying mechanism of MIT with different thicknesses of 2D channels. Therefore, the objective of this study was to systematically investigate the MIT behavior observed in 2D WSe<sub>2</sub> devices by varying the thickness

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of the WSe<sub>2</sub> flake from ~20 to 0.73 nm (monolayer), different from previous studies.<sup>[23,27,29]</sup> We carried out multifrequency capacitance–voltage (MFC-V) and transport measurements with temperatures ranging from 300 to 75 K to determine the effect of interface quality and correspondingly localized  $D_t$  on MIT. Since MFC-V measurements carried out by applying different excitation frequencies (1 kHz to 1 MHz in this study) provide direct insight about localized  $D_t$ , they are considered the most appropriate and powerful technique to analyze the channel-gate dielectric interface and its impact on device characteristics.<sup>[22,31–33]</sup>

This thickness-dependent systematic analysis provided an interesting clue that the MIT point strongly depended on flake thickness. The corresponding critical carrier density  $(n_c)$ at the transition point significantly increased with reducing WSe<sub>2</sub> channel thickness. These tunable characteristics of WSe<sub>2</sub> devices can be used for fast optoelectronic switches by utilizing the difference in optical transmission between insulating and metallic regions. To further understand this thicknessdependent tunable transition in WSe<sub>2</sub> devices, we analyzed the interface between the channel (WSe<sub>2</sub>) and gate dielectric (hBN) by estimating localized  $D_t$  in all measured devices. We found that the occurrence of MIT in WSe<sub>2</sub> devices strongly depended on the interface quality and corresponding localized  $D_t$  at the interface. Moreover, we analyzed our data of WSe<sub>2</sub> devices with different thickness of WSe2 flake by employing the percolation model of conductivity. Based on thickness-dependent percolation analysis that follows the principle of power-law (i.e.,  $\sigma(n) = A(n - n_{cn})^{\delta}$ ), we obtained values of percolation exponent  $\delta \approx 1.377 \pm 0.013$  to  $1.4257 \pm 0.022$  for monolayer (0.73 nm) and  $\delta \approx 1.743 \pm 0.057$  to  $1.966 \pm 0.052$  for few layers (3.16nm) in WSe<sub>2</sub> devices at measured temperatures of 75 to 300 K. These obtained values of  $\delta$  in WSe<sub>2</sub> devices using up to a few layers of WSe<sub>2</sub> are close to the expected  $\delta$  value in 2D materials, suggesting that MIT occurring in thinner (up to a few layers) WSe<sub>2</sub> devices is a percolation driven transition. In contrast, transport data of multilayer WSe<sub>2</sub> devices did not obey the percolation theory, implying that interaction-dominant MIT occurred in multilayer WSe<sub>2</sub> devices. In addition, the Wigner–Seitz radius ( $r_{\rm s}$ ) significantly decreased from  $\approx 8.60$  to 2.20 with decreasing flake thickness from multilayers to monolayer. This also indicates that Coulomb interaction between carriers becomes weaker with decreasing thickness and the system highly becomes disordered.

## 2. Results and Discussions

**Figure 1**a,b illustrates schematic and optical images of a specially designed van der Waals bottom contact field-effect transistor (FET) fabricated by transferring mechanically exfoliated flakes of WSe<sub>2</sub> and hBN on the pre-deposited source and drain electrodes (Pt) on a p-type silicon substrate coated with 285 nm SiO<sub>2</sub>. Further details of the van der Waals bottom contact FET fabrication process are given in the device fabrication section, and S1 of Supporting Information. Here, we used pre-deposited bottom electrodes to avoid chemical disorder and crystal defects induced by direct lithography and metal deposition on the WSe<sub>2</sub> channel. The equivalent circuit of devices shown in Figure 1c demonstrates total measured capacitance (*C*) resulting from the



**Figure 1.** Device fabrication details and frequency-dependent capacitance-voltage measurements. a–c) Schematic image and optical image, and an equivalent circuit of the top gate van-der-Waal bottom contact WSe<sub>2</sub> field-effect transistor, respectively. d,e) show the capacitance-voltage characteristics obtained from a monolayer (0.73 nm) and multilayer (6.41 nm) WSe<sub>2</sub> devices at various frequencies, respectively, where the dotted pink verticle line indicates the flat band voltage ( $V_{FB}$ ). Thickness height profiles of WSe<sub>2</sub> flakes taken by AFM of respective devices are shown in the inset of (d) and (e).

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collective effect of the hBN ( $C_{hBN}$ ) and WSe<sub>2</sub> ( $C_{WSe2}$ ) in serial connection plus parasitic capacitance ( $C_p$ ) and trap induced capacitance ( $C_t$ ) in parallel connection. For further details about  $C_p$  and the equivalent circuit, see Figures S2 and S3 (Supporting Information), respectively. Before electrical characterization, we carried out atomic force microscopy (AFM) analysis to ascertain the thickness of flakes and surface roughness. AFM height profiles are shown in the inset of Figure 1d,e. Details are given in Figures S4 and S5 (Supporting Information).

#### 2.1. Capacitance-Voltage Measurements

Multifrequency capacitance-voltage (MFC-V) measurements<sup>[32]</sup> were carried out inside a vacuum chamber using an LCR meter by applying the gate voltage  $(V_G)$  and varying the applied frequency from 10 kHz to 1 MHz at room temperature (RT) on WSe<sub>2</sub> devices with the thickness of WSe<sub>2</sub> flake varying from ≈20 to 0.73 nm (monolayer). Extra efforts were put to use similar thickness≈20 nm of the hBN flakes. Figure 1d,e shows MFC-V results of monolayer and 6.41 nm thick WSe2 devices, respectively. When  $V_{\rm G}$  is smaller than  $V_{\rm FB}$  (where  $V_{\rm FB}$  is flat band voltage), holes accumulated at the WSe2/hBN interface and the obtained capacitance approached hBN capacitance  $C_{\text{max}} = C_{\text{hBN}}$ . Whereas when  $V_{\rm G}$  is larger than  $V_{\rm FB}$ , holes started to deplete from the WSe2/hBN interface and the measured capacitance becomes  $C_{min} = \frac{C_{hBN} C_{WSe_2}}{C_{hBN} + C_{WSe_2}}$  in the deep depletion region. The obtained  $V_{FB}$  of  $\approx$ - 9.3V for 0.73 nm and - 2.79V for 6.41 nm thick WSe<sub>2</sub> devices estimated by employing the graphical-based

method.<sup>[34,35]</sup> For details see Figure S6 (Supporting Information). Frequency dispersion in the depletion region is attributed to the presence of traps at the WSe<sub>2</sub>/hBN interface.<sup>[22,32,33]</sup> Furthermore, the traps at the WSe<sub>2</sub>/hBN interface will be discussed later by quantifying the localized traps density ( $D_{\rm t}$ ).

We then performed temperature-dependent measurements in the range of 75 to 300 K with a step of 25 K to examine the response of capacitance-voltage (C-V) of the above-mentioned thickness range (20 nm to monolayer) of WSe2 devices. C-V curves of WSe2 devices with different thicknesses obtained at various temperatures showed an interesting metal-insulator transition (MIT) phenomenon at a certain  $V_{\rm G}$ .<sup>[23,24]</sup> For example, 7.23 nm and 3.16 nm thick WSe<sub>2</sub> devices show MIT points at  $V_{\rm C}$ of = -3.6V and -6.4V as shown in Figures 2a,b, respectively. Below the MIT point, the capacitance increased with increasing temperature, indicating the formation of an insulating phase. However, above the MIT point, temperature dependency is the opposite, showing characteristic of the metal. To visualize the change in capacitance with V<sub>G</sub> and temperature, we mapped capacitance data of 7.23 nm thick WSe<sub>2</sub> devices as shown in Figure 2c. The color plot data confirmed distinct regions:  $\Delta C/\Delta T > 0$  when  $V_G \approx >-3.6$  V indicating insulating phase,  $\Delta C/\Delta T \approx 0$  at V<sub>G</sub>  $\approx -3.6$  V suggesting temperature-independent point, and  $\Delta C/\Delta T < 0$  when  $V_G \approx <-3.6$  V showing the metallic phase. The corresponding critical carrier density  $(n_c)$  at MIT point is  $n_c \approx 2.08 \times 10^{12} \text{ cm}^{-2}$  ( $V_G = -3.6 \text{ V}$ ) for 7.23 nm thick WSe<sub>2</sub> and  $n_c \approx 6.81 \times 10^{12} \text{ cm}^{-2}$  ( $V_G = -6.4 \text{ V}$ ) for 3.16 nm thick flake. It is estimated with  $n_{2D} = \frac{C_{ox}(V_G - V_{th})}{q}$ , where  $C_{ox}$  is the oxide capacitance per unit area, V<sub>th</sub> is the threshold voltage,



**Figure 2.** Metal–insulator transition driven by traps. a,b) Capacitance–voltage curves of  $\approx$ 7.23 nm and 3.16 nm thick WSe<sub>2</sub> devices measured at various temperature points, respectively, where the dotted black vertical line indicates the MIT point . c) Color-code plots of the 7.23 nm think WSe<sub>2</sub> device. d) Critical carrier density ( $n_c$ ) and corresponding trap density ( $D_t$ ) versus thickness of WSe<sub>2</sub> flake ( $t_{WSe_2}$ ).



and q is the elementary charge.<sup>[23,36]</sup> The  $V_{\rm th}$  is estimated from the linear region of the C-V curve (see Figure S7, Supporting Information).<sup>[24,36]</sup> Interestingly, we noticed that the transition point was dependent on WSe2 flake thickness. It shifted toward a higher  $V_{\rm G}$  with reducing WSe<sub>2</sub> channel thickness. To further confirm this, we tried more thickness variations and plotted the estimated  $n_c$  as a function of WSe<sub>2</sub> ( $t_{WSe2}$ ) thickness in as shown Figure 2d. Surprisingly, results showed that  $n_c$  monotonically decreased from  $\approx 9.45 \times 10^{12}$  to  $8.30 \times 10^{11}$  cm<sup>-2</sup> as  $t_{WSe2}$ . increased from monolayer to ≈20 nm. This unique trend indicates a promising thickness dependent tunable MIT characteristics in WSe<sub>2</sub> devices. Previously, MIT observed in 2D materials has been explained by carrier-carrier interactions and considered as the fundamental origin of MIT in a 2D system.<sup>[23,24,27,28]</sup> In contrast, 2D materials-based devices are strongly influenced by localized trap charges induced at channel-gate dielectric interface and defects.<sup>[8,9]</sup> Both carrier-carrier interaction and large trap density coexist in 2D layered materials. Their relative strengths can be further modulated by controlling the thickness of the 2D channel. In principle, interactions increase with increasing thickness of the 2D channel while trap density decreases. To understand the fundamental origin of MIT phenomena in 2D materials both effects (carrier-carrier interaction and trap density) should be considered. Therefore, to correctly analyze the MIT phenomena in WSe<sub>2</sub> devices different thicknesses, we considered the impact of localized D<sub>t</sub> including interface traps and defects near the interfaces for the aforementioned thickness range in the subsequent discussion.

We estimated localized D<sub>t</sub> from MFC-V measurement results with different excitation frequencies (f). These different excitation frequencies can excite the charge trap states when  $1/f > \tau_t$ (where  $\tau_t$  is the relaxation time of localized charge traps) and contribute to the measured capacitance. Whereas when  $1/f < \tau_t$ , charge trap states are unable to follow high frequencies. Therefore, localized  $D_t$  can be determined by capacitances measured at low and high excitation frequencies using  $D_{t} = \frac{1}{qA} \left[ \left( \frac{1}{C_{\text{low f}}} - \frac{1}{C_{hBN}} \right)^{-1} - \left( \frac{1}{C_{\text{high f}}} - \frac{1}{C_{hBN}} \right)^{-1} \right] = \frac{C_{t}}{qA}, \text{ where } C_{\text{low f}}$ and  $C_{\text{high f}}$  are the capacitance at low and high excitation frequencies, respectively,  $C_t$  is the trap capacitance, and A is the area of the capacitor.<sup>[31-33]</sup> Estimated D<sub>t</sub> values at the MIT point drastically increased from  $\approx 6.02 \times 10^{11}$  to  $1.13 \times 10^{13}$  cm<sup>-2</sup> eV<sup>-1</sup> as  $t_{WSe2}$  changed from  $\approx 20$  nm to monolayer as shown in Figure 2d. These obtained results indicate that thinner flakes are more susceptible to interface disorders due to large surface-to-volume ratios<sup>[37]</sup> and higher susceptibility to immediate environment induced roughness.<sup>[38]</sup> The localized D<sub>t</sub> in WSe<sub>2</sub> devices can arise due to material imperfections such as chalcogen vacancies, transition metal vacancies, anti-sites (when the transition metals occupy chalcogen vacancy), dislocation, dielectric-induced defects, device processing-induced defects, and strain induced from the substrate.<sup>[39,40]</sup> These localized  $D_t$ play a significant role in altering the transport characteristic of WSe<sub>2</sub> devices through hopping between localized states that could be explained by the variable-range-hopping model.<sup>[41,42]</sup> In addition, these localized  $D_t$  can smear inside the bandgap and alter the band structure as well as the doping profile in 2D semiconducting materials, resulting in electrical behavior strongly affected by these trap charges.<sup>[31,40,43]</sup> Therefore, a compromised



electrical performance, such as degradation in mobility,[31,38] strong Fermi level pinning,<sup>[44]</sup> and large subthreshold swing,<sup>[6]</sup> is understandable for thinner 2D flakes as compared to thicker flakes. Similarly, the current experimental study revealed that MIT observed in WSe<sub>2</sub> devices was strongly dependent on WSe<sub>2</sub> channel thickness and corresponding WSe2/hBN interface quality. This suggests that the physical origin of MIT observed in WSe<sub>2</sub> devices with different thicknesses is associated with the strength of localized Dt and interface perturbation. The impact of these interface perturbations can be increased by reducing flake thickness where large localized D<sub>t</sub> is observed. The localized  $D_t$  can lead to generate strong potential fluctuations in the band of WSe2 due to randomly occupied charge traps at the interfaces. Consequently, different kinds of transition mechanisms are expected for WSe<sub>2</sub> devices with different thicknesses depending on the influence and strength of D<sub>t</sub>.<sup>[17,45]</sup> Further investigation of  $D_t$  effect on MIT is discussed below by analyzing electrical transport data.

#### 2.2. Electrical Transport Measurements

The thickness-dependent MIT in WSe<sub>2</sub> devices was further confirmed by electrical transport measurements as shown in **Figure 3.** Conductivities ( $\sigma = (\frac{I_D}{V_D} \times \frac{L}{W})$  where *L*, and *W* are the channel length and width respectively) as a function of  $V_{\rm G}$  of 7.23 nm and 4.31 nm thick WSe2 devices at different temperatures showed well-defined crossover points at  $V_{\rm G}$  of - 3.6 and - 5.4V as shown in Figures 3a,b, respectively. The MIT behavior was observed in measured devices approximately the same  $V_{\rm G}$ from both C-V and transport measurements, ensuring the reliability and repeatability of the data for WSe<sub>2</sub> devices. Transport data for both devices also clearly indicated that  $\sigma$  increased with decreasing temperature when  $V_{\rm G}$  is higher than - 3.6V and -5.4V for 7.23 nm and 4.31 nm devices, respectively, showing the metallic behavior while  $\sigma$  showed the opposite behavior when  $V_{\rm G}$  is lower than – 3.6 V and – 5.4 V for 7.23 nm and 4.31 nm devices respectively, indicating the insulating phase, as shown in the inset of Figure 3a,b. To see more clearly the critical transition point from transport measurements, we plotted temperature-dependent  $\sigma$  for different V<sub>G</sub> values with corresponding  $n_{2D}$  for 7.23 nm and 4.31 nm devices as shown in Figures 3c,d, respectively. It is clearly shown that  $\sigma$  increased with decreasing temperature attributed to the metallic behavior when  $n_{2D}$ greater than  $n_c$  (2.08 × 10<sup>12</sup> cm<sup>-2</sup>) and corresponding localized trap density  $D_{\rm t} \approx 3.67 \times 10^{12} \text{ cm}^{-2} \text{ eV}^{-1}$  for 7.23 nm device and when  $n_c \approx 5.44 \times 10^{12} \text{ cm}^{-2}$  and  $D_t \approx 6.72 \times 10^{12} \text{ cm}^{-2} \text{ eV}^{-1}$  for 4.31 nm device. In contrast,  $\sigma$  showed the opposite trend when  $n_{\rm 2D}$  and localized  $D_{\rm t}$  were smaller than the above values for both devices.

To evaluate disorders and unavoidable scatterings induced by interface traps, field-effect mobility ( $\mu$ ) is an important physical parameter of the measured devices. We extracted field-effect mobility ( $\mu$ ) using the following equation:  $\mu = \left(\frac{L}{WC_GV_D}\right) \left(\frac{dI_D}{dV_G}\right)$ , where  $C_G$  are the gate capacitance per unit area measured in the accumulation region of the C–V curve. The estimated  $\mu$  at the transition point ( $\mu_c$ ) and the corresponding localized  $D_t$ 







**Figure 3.** Thickness-dependent tunable MIT in WSe<sub>2</sub> devices. a,b) Conductivity versus applied gate voltage at different temperatures for  $\approx$ 7.23 and 4.31 nm WSe<sub>2</sub> devices, respectively. Insets show conductance versus applied gate voltage in the semilogarithmic scale, where the black dotted vertical line represents transition points and arrow indicates the corresponding critical carrier densities ( $n_c$ ). c,d) Conductivity versus temperature at different gate voltages, showing metallic and insulating phases of 7.23 and 4.31 nm WSe<sub>2</sub> devices, respectively. e) Critical mobility ( $\mu_c$ ) and corresponding trap density ( $D_t$ ) as a function of the thickness of WSe<sub>2</sub> flake ( $t_{WSe_2}$ ) measured at 223 K. f) Mobility versus temperature for 7.23 and 4.31 nm WSe<sub>2</sub> devices, where solid black lines serve as guidelines for the  $\mu \approx T^{-\gamma}$  relation.

as a function of respective thickness as shown in Figure 3e. They were used to determine the direct impact of localized  $D_t$  on the transport at the MIT point. The  $\mu_c$  was decreased significantly from  $\approx$ 47 to 11 cm<sup>-2</sup> V<sup>-1</sup> s<sup>-1</sup> when the WSe<sub>2</sub> channel thickness was decreased from multilayers ( $\approx$ 8.2 nm) to monolayer ( $\approx$ 0.73 nm) while the corresponding localized  $D_t$  strongly increased from 2.35 × 10<sup>12</sup> to 1.12 × 10<sup>13</sup> cm<sup>-2</sup> eV<sup>-1</sup>. This drastic decreasing trend of  $\mu_c$  was attributed to a significant increment in the localized  $D_t$  with reducing WSe<sub>2</sub> channel thickness. This confirms that the transport at the transition point is strongly controlled and modulated by localized  $D_t$  in the respective device, consistent with the previous reports showing the impact of substrate trap states on carrier  $\mu$  in 2D materials was observed.<sup>[6,38,46]</sup>

Figure 3f shows mobility versus temperature obtained for 7.23 and 4.31 nm WSe<sub>2</sub> devices. Initially,  $\mu$  increased until it reached a maximum value as the temperature increased from 75 to 223 K. It then decreased with the further increase of temperature. This suggests that the  $\mu$  of a WSe<sub>2</sub> depends on different scattering mechanisms and distribution of localized  $D_{\rm t}$ . Theoretically, mobility is determined by intrinsic electron-phonon coupling at higher temperatures, often known as phonon limited  $\mu$ . However, experimentally observed  $\mu$  values are predominately limited by several external factors such as defects, Coulomb impurities, and localized  $D_{\rm t}$  at the

channel-gate dielectric interface as a major factor.<sup>[23,38,47]</sup> In addition, we fitted results of  $\mu$  versus temperature to the relation of,  $\mu \approx T^{-\gamma}$ , where  $\gamma$  is the critical exponent that depends on scattering. The fitted value of  $\gamma$  is – 1.30 for 7.23 nm and – 1.20 for 4.31 nm devices at temperatures greater than 223 K, suggesting that the electron scattering is due to optical phonons. For temperatures lower than 223 K, the fitted value of  $\gamma$  is 0.433 for 7.23 nm and 0.595 for 4.31 nm, indicating the presence of charge impurity scattering at the interface.

The occurrence of MIT in 2D semiconductors can be further confirmed by the Ioffe–Regel criterion.<sup>[11,23,48]</sup> According to this criterion, the MIT can be observed in the system when parameters  $k_F l \approx 1$ . The system would be at the metallic phase for  $k_F l >> 1$  whereas the system considered an insulator when  $k_F l << 1$ . Here,  $k_F = \sqrt{2\pi n_{2D}}$  is the Fermi wave vector and  $l = \frac{\hbar k_F \sigma}{n_{2D} q^2}$  is the mean free path of the carrier. The estimated  $k_F l \approx 1.65$  was obtained at transition point of  $V_G = -3.6V$  for 7.23 nm WSe<sub>2</sub> device, showing a good agreement with the loffe–Regel theory. Our other measured WSe<sub>2</sub> devices also exhibit  $k_F l$  close to 1.6, values in different regions (insulating, near MIT point and metallic,) for different thicknesses are given in Supporting Information S8 and Tables S1–S3 (Supporting Information). In addition, we estimated the Fermi temperature (i.e.,  $T_F = \frac{\pi \hbar^2 n_c}{k_B m^*}$ )





at the MIT point for different thickness devices using the value of  $n_c$  given in Figure 2d. Here,  $m^*$  is the effective mass,  $k_B$  is the Boltzmann constant, and h is the Plank constant. We obtained Fermi temperatures in the range of  $\approx 69$  to 773 K for different thickness WSe<sub>2</sub> devices using the respective  $n_c$  from  $8.30 \times 10^{11}$  to  $9.45 \times 10^{12}$  cm<sup>-2</sup> and considering  $m^* = 0.34 m_o$ .<sup>[49]</sup> Further details are given in Supporting Information S9 and Table S4 (Supporting Information). Previously, Fermi temperature from 56 to 556 K in a few layers ReS<sub>2</sub> has been reported.<sup>[27]</sup> The slightly large value of  $T_F$  obtained in this study is due to different values of  $m^*$  and  $n_c$  for different thicknesses.

#### 2.3. Thickness-Dependent Percolation Critical Behavior

According to the scaling theory of localization, a carrier-carrier interaction in the system can be determined by the strength of Coulomb interaction between carriers. In the presence of localized  $D_t$ , the strength of Coulomb interaction is characterized by the Wigner-Seitz radius  $(r_s)$ , defined as the ratio of potential (coulomb,  $E_C$ ), and kinetic (Fermi,  $E_F$ ) energy by  $r_s = \frac{E_C}{E_F} = \frac{n_v}{a^* \sqrt{\pi n_{2D}}} = \frac{m^* e^2 n_v}{4\pi \epsilon \hbar^2 \sqrt{\pi n_{2D}}}$ , where  $n_v$  represents the number of degenerate valleys,  $a^*=4\pi \epsilon \hbar^2 /m^* e^2$  is the effective Bohr radius, and  $\epsilon$  is the dielectric constant of the material.<sup>[23]</sup> A system can be considered strongly interacting if the  $r_s >> 1.^{[50]}$  Therefore, we calculated values of  $r_s$  at the transition point for WSe<sub>2</sub> devices with different thicknesses to figure out the variation in interaction strength depending on flake thickness. Estimated values of  $r_s$  at MIT point ranged from  $\approx 8.60$  to 2.20 as

the thickness decreased from ≈8.2 nm to 0.73 nm (monolayer) considering thickness dependent  $m^*$  and  $\varepsilon$  reported by Wickramaratne et al. and Jeon et al., respectively.<sup>[49,51]</sup> The decreased Coulomb interaction is due to the increasesd  $D_t$  and  $n_c$  and decreased  $m^*$  and  $\varepsilon$  with decreasing flake thickness. Estimated values of r<sub>s</sub> at MIT point for WSe<sub>2</sub> devices with different thicknesses is slightly different from those previously reported in the case of MoS<sub>2</sub> due to relatively high  $m^*$  and different  $\varepsilon$  of  $MoS_2$ .<sup>[23]</sup> The significantly decreased value of  $r_s$  clearly indicates that the Coulomb interaction between carriers becomes weaker with reducing flake thickness. Consequently, the strength of the localized  $D_t$  governs the system. In the presence of high localized Dt, the MIT in different 2D systems can be analyzed by the percolation model of conductivity.<sup>[26,30,52]</sup> Therefore, we analyzed the percolation model of conductivity for all measured devices having different thicknesses of WSe<sub>2</sub> flakes to provide further insight into the thickness-dependent tunable MIT in WSe<sub>2</sub> devices.

The conductivity in percolation driven transition is expressed by a power law to carrier density by  $\sigma$  (n) = A(n – n<sub>cp</sub>)<sup> $\delta$ </sup>, where *A*,  $\delta$  and  $n_{cp}$  are the constant of proportionality, critical percolation exponent, and critical carrier density respectively.<sup>[24,53]</sup> Measured  $\sigma$  values of multilayers (7.23 nm), few layers (3.16 nm), and monolayer (0.73 nm) WSe<sub>2</sub> devices are given in **Figure 4**a. Based on power-law fitting,  $\delta$  values of 1.377 ± 0.013 to 1.4257 ± 0.022 for monolayer (0.73 nm) and 1.743 ± 0.057 to 1.966 ± 0.052 for few-layer (3.16 nm) were obtained within the measured temperature range of 75 to 300 K, close to the 2D percolation exponent value of 1.33. <sup>[30,52,53]</sup> Obtained values of  $\delta$  from the fitting of power-law at different temperatures for



**Figure 4.** Thickness-dependent percolation analysis. a) The fitting of measured conductivity as a function of carrier density for multilayer (7.23 nm), few-layer (3.16 nm), and monolayer (0.73 nm) WSe<sub>2</sub> devices was performed using the percolation model of  $\sigma$  (n) =  $A(n - n_{cp})^{\delta}$ . The orange arrow in the vertical direction represents the position of MITs. b,c) Variation of critical percolation exponents ( $\delta$ ) and critical carrier density obtained by percolation fitting for different thickness devices. The dotted red lines in (b) represent expected values of  $\delta$  in the 2D material system.



devices with different thicknesses are shown in Figures 4b. We found an excellent agreement between the measured conductivity data and the theoretical model for WSe2 devices when WSe<sub>2</sub> flakes were used up to a few layers. Therefore, we believe that the MIT observed in WSe<sub>2</sub> devices using up to a few layers of WSe<sub>2</sub> flake is due to charge density inhomogeneity caused by potential fluctuation induced by localized Dt which leads to a percolation-driven transition. However, in the case of multilaver WSe<sub>2</sub> devices, value of  $\delta$  were 2.586 ± 1.366 to 3.293 ± 1.701, indicating that the percolation theory is no longer valid in the multilayer WSe<sub>2</sub> system and that the transition is likely to be led by carrier-carrier interactions. Such deviations with increasing the thickness of WSe<sub>2</sub> flakes indicate that the nature of the transition strongly depends on the relative strength of localized Dt and carrier-carrier interactions depending on the thickness of WSe<sub>2</sub> flakes and interface perturbation. In addition, it is important to point out that the value of  $n_{\rm CD}$ extracted from the theoretical model is lower than the corresponding estimated value of  $n_c$  at the MIT cross-over point from experimental data for all devices. Estimated  $n_{\rm cp}$  values at different temperatures for different device thicknesses are shown in Figure 4c. At 75K,  $n_{\rm cp}$  was  $\approx 8.84 \times 10^{10}$  cm<sup>-2</sup> and  $n_{\rm c}$ was $\approx 2.08 \times 10^{12}$  cm<sup>-2</sup> for 7.23 nm (multilayer) device,  $n_{cp}$  was  $\approx 1.3 \times 10^{12} \text{ cm}^{-2}$  and,  $n_c$  was  $\approx 6.81 \times 10^{12} \text{ cm}^{-2}$  for 3.16 nm (few layers) device, while  $n_{\rm cp}$  was  $\approx 1.9 \times 10^{12}$  cm<sup>-2</sup> and  $n_{\rm c}$  was  $\approx 9.45 \times 10^{12}$  cm<sup>-2</sup> for the monolayer device. The difference in critical carrier density between theoretical and experimental data is due to thermal activation of localized states and hopping conductivity at finite temperature.<sup>[28]</sup>

Findings of this study suggest that disorders induced by localized traps at interfaces and carrier–carrier interactions are both important parameters to analyze MIT in WSe<sub>2</sub> devices depending on the thickness of the WSe<sub>2</sub> flake. Because the thickness of the 2D flake primarily determines the relative strength of disorders and carrier-carrier interactions in the system, it controls the transition mechanism in a 2D layered system. We plotted  $D_t$  and  $r_s$  obtained at MIT point as a function of  $t_{WSe2}$  as shown in **Figure 5a**. When the WSe<sub>2</sub> channel thickness was downsized from few-layers to a monolayer (light yellow shaded area in Figure 5a) disorders might have prevailed over the carrier–carrier interactions, leading to a disorder-dominated transition. In contrast, the transition observed in multilayer WSe<sub>2</sub> devices was possibly interaction dominated as



evidenced by the large value of Coulomb interaction shown in the light green shaded area in Figure 5a. Lastly, to qualitatively understand the formation of random potential fluctuations from localized trapped charges at the WSe<sub>2</sub>/hBN interface, a comprehensive energy band diagram is driven for WSe<sub>2</sub> as shown in Figure 5b. In thinner WSe<sub>2</sub> devices below a few-layers where percolation theory is obeyed, disorder-induced localized *D*<sub>t</sub> and screening in a device play a significant role. High localized Dt values in thinner devices can lead to large interface perturbations and high inhomogeneous electronic potential landscape which can effectively control the transport behavior of the device. In addition, the screening of these trapped charges becomes weaker due to the large bandgap of WSe<sub>2</sub> unlike at graphene system.<sup>[45]</sup> With increasing flake thickness the localized D<sub>t</sub> decreases and screening of these trapped charges can be increased. Consequently, less potential fluctuation in the band of WSe<sub>2</sub> is expected.

## 3. Conclusion

We performed a detailed analysis of thickness-dependent MIT in WSe<sub>2</sub> devices by varying the WSe<sub>2</sub> channel thickness from 20 to 0.73 nm (monolayer). We observed that MIT in WSe<sub>2</sub> devices was strongly dependent on channel thickness and the corresponding localized  $D_t$  at the WSe<sub>2</sub>/hBN interface. The estimated critical carrier density  $(n_c)$  at the transition point significantly increased with the decreasing thickness of WSe<sub>2</sub> flakes, attributed to dramatically increased localized  $D_t$  in thinner devices. Furthermore, we found an excellent agreement between experimentally measured conductivity data and theoretical percolation model for WSe2 devices with WSe<sub>2</sub> flakes having thickness up to a few-layers. This suggests that the percolation type MIT is the dominant mechanism in thinner WSe2 devices due to the random potential fluctuation caused by large localized  $D_t$  at the interface. In contrast, the percolation theory is no longer valid in multilayer WSe<sub>2</sub> devices as the transition is likely driven by carrier-carrier interactions. This is also confirmed by the large strength of Coulomb interaction estimated by the Wigner-Seitz radius. These findings indicate that tunable MIT with the thickness of flake in layered WSe2 would be a strong candidate for engineering phase change-based devices such as non-volatile



**Figure 5.** Summary of transition mechanism. a) Variation of trap density ( $D_t$ ) and Wigner–Seitz radius ( $r_s$ ) estimated at MIT point for WSe<sub>2</sub> devices with different thicknesses. The light-yellow shaded area represents localized trap dominated region (below few layers of WSe<sub>2</sub>) light green area represents multilayers where interaction is the dominant mechanism of transition. b) Schematic to illustrate the distribution of localized  $D_t$  with corresponding possible random potential fluctuation WSe<sub>2</sub> devices with different thickness.

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memory devices as it can be used to control and tune the transition point by controlling the thickness of flakes.

#### 4. Experimental Section

Device Fabrication: A van der Waals bottom contact field-effect transistor (FET) was fabricated, as shown in Figures 1a,b. First, to deposit bottom electrodes, a pre-pattern was designed on a p-Si/SiO<sub>2</sub> substrate by standard electron-beam lithography, and 5/25 nm thick Cr/Pt metal electrodes were deposited by electron-beam evaporation under high vacuum ( $8 \times 10^{-8}$  Torr) to ensure good electrical contacts. The mechanically exfoliated WSe<sub>2</sub> from bulk  $\approx$ 20 nm thick to monolayer was picked with a 20 nm thick hBN flake and transferred onto the prepatterned electrode with a dry transfer method using an auto-transfer stage inside a glove box with moisture and oxygen concentration < 1 ppm, which enabled to avoid the formation of bubbles and chemical residues at the WSe<sub>2</sub>/hBN interface. Finally, the top gate Cr/Au metal electrode of 5/70 nm thickness was deposited to complete the device fabrication.

*Device Characterization*: After completing the fabrication process, electrical (current-voltage and capacitance-voltage) measurements were conducted using a semiconductor parameter analyzer (Agilent 4155C) and an LCR meter (Agilent E4980A) in a vacuum chamber with varying temperatures from 300 to 75 K.

Atomic Force Microscopy (AFM). All the AFM analyses were performed at room temperature under atmospheric pressure by placing the sample on a metal puck that was grounded.

## **Supporting Information**

Supporting Information is available from the Wiley Online Library or from the author.

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## **Conflict of Interest**

The authors declare no conflict of interest.

## **Data Availability Statement**

The data that support the findings of this study are available in the supplementary material of this article.

## Keywords

capacitance–voltage (C—V), low-temperature measurement, transport (I—V) measurements, trap density ( $D_t$ ), tunable metal-insulator transition (MIT), WSe<sub>2</sub> thicknesses

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